

control 03

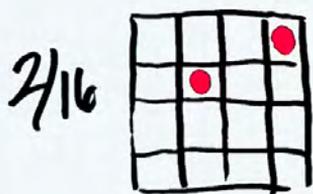
COSS 300

Feb 03/26

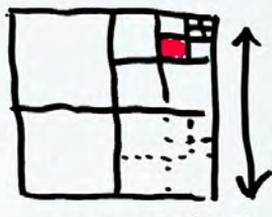
①

Warm up: discretizations + tiling.

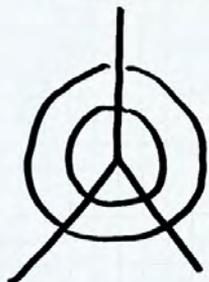
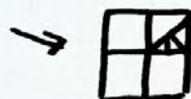
Create different "grids": \longleftrightarrow



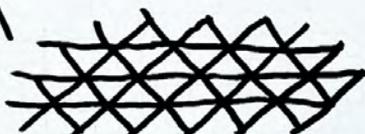
cartesian



recursive



polar



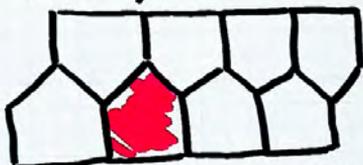
triangular



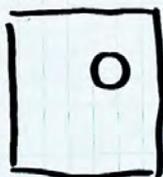
1D
linear

etc...

$1/8$



pentagon-ish



p (point is covered)?

$r = 1 \text{ cm}$

$A = 21 \times 29.7 \text{ cm}^2$



← 22 →



$$22 \times 33 = 726$$

$$\frac{\pi r^2}{A} = \frac{1}{623.7}$$

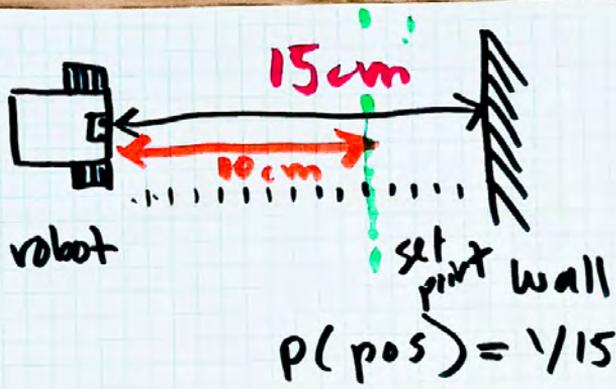
0.0016
↑

$$\frac{1}{150} \quad \text{---} \quad \frac{1}{726}$$

$$r = 1 \text{ cm}$$

$$A = 21 \times 29.7 \text{ cm}^2$$

3



go faster the farther we are
slower closer

out = map (dist, min, max, lo, hi);

PID = proportional integral derivative

current pos = pos = read();

set point = set = 5 cm;

error = pos - set;

output = out = c · error

"tuning"

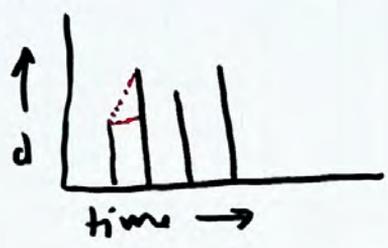
err = 1 cm
 out = 500

c = 500 err = 10
 out = 5000

c = 100	err = 10	out = 1000
c = 100	err = 1	out = 100
c = 17	err = 10	out = 170
c = 17	err = 1	out = 17

Simulation + tuning

d_0
 d_1
 d_2
 \vdots
 d_n

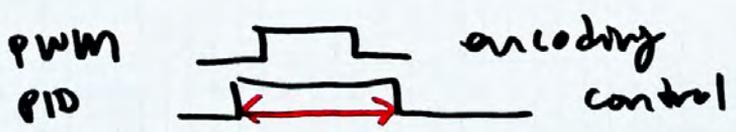


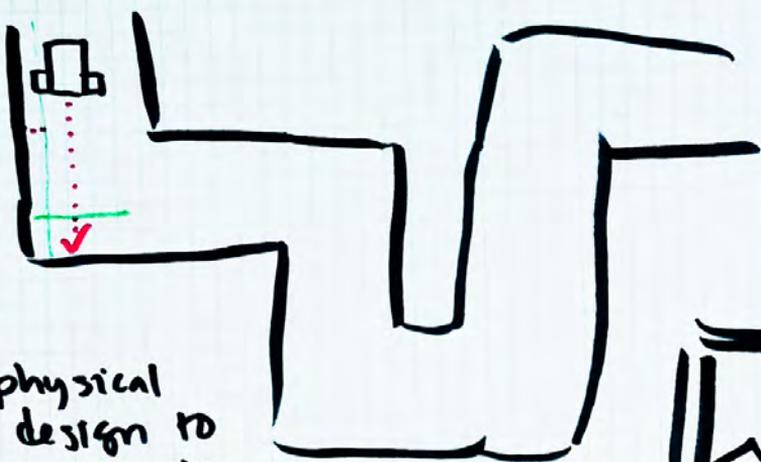
$$\frac{d_j - d_i}{1} = d_j - d_i$$

$$\Delta d$$

$$c \cdot \text{error} + a \cdot \Delta \text{error} + b \cdot \sum \text{error}$$

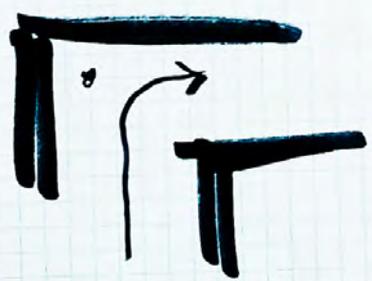
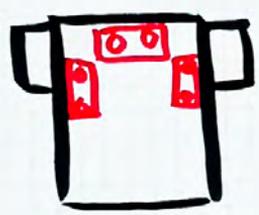
P
D
I





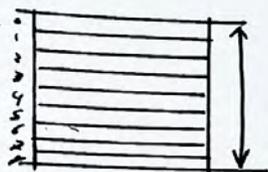
1. physical design to sense in maze

2. Algorithm for control

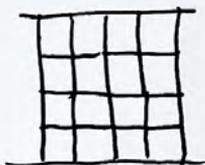


Control 03

Warm-up: Discretizations + tiling



linear



cartesian



polar

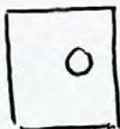


recursive cartesian



triangular

probability: if I throw a coin onto a page, $P(\text{point is covered})$

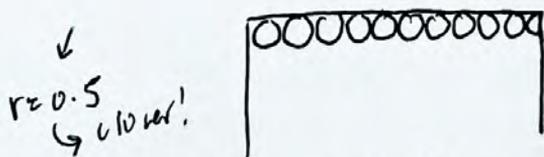


$$\frac{\text{area of coin}}{\text{area of page}} ?$$

$$p = \frac{\pi r^2}{A} = 1/623.7$$

$$r = 1 \text{ cm}$$

$$A = 21 \times 29.7 = 623.7$$

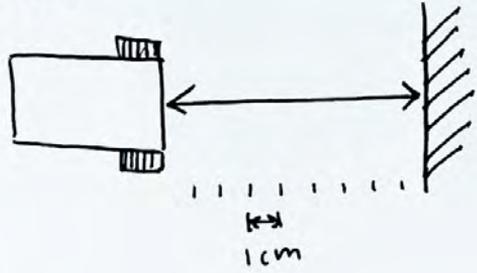


try it!
 ← 10 →
 15 ↑ ↓

$$0.0066 \sim 0.0016 ?$$

$$\longleftrightarrow 1/150 \sim \frac{1}{623.7} ?$$

Robot.



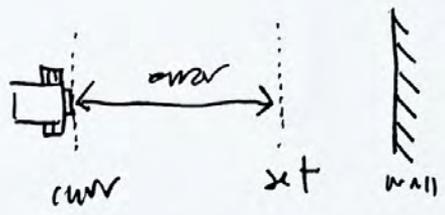
$$\begin{aligned}
 &P(\text{Robot is @ } 5\text{cm}) \\
 &= 1/10 \\
 &= \frac{1\text{cm chunk}}{\# \text{ of chunks}}
 \end{aligned}$$

↳ robot doesn't "know," it has to guess.

Last time: alg. for driving to set point.

Key insight: go faster, further.

$$\text{output} = \text{map}(\text{dist to set point, min dist, max dist, min motor, max motor}).$$



$$\begin{aligned}
 &\text{error} = \text{curr} - \text{set}; \\
 &\text{output} = \text{map}(\text{error}, 0, 10, 0, 255);
 \end{aligned}$$

↳ but what about a diff. curve?

③

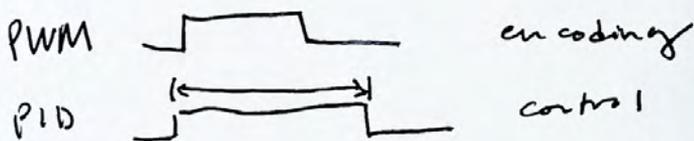
```
curr = read();  
set = 5 cm; // cm  
error = curr - set;  
out = curr C * error  
      ↑  
      some constant
```

$C = 100$ $err = 5$ $out = 500$

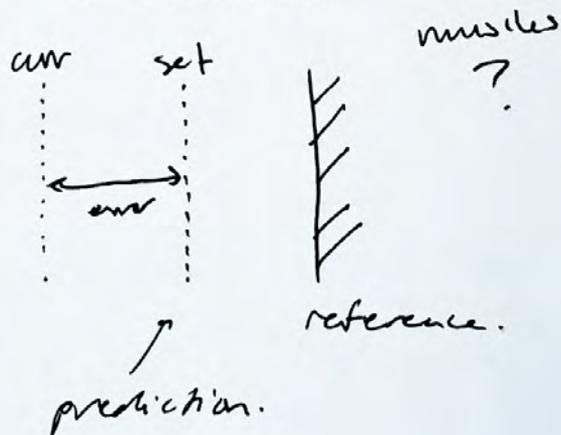
$C = 50$ $err = 5$ $out = 250$

$C = 1/5$ $err = 5$ $out = 1$

depends on your robot.



control requires sensation + model.
to evaluate.



④

★ come up with a wall-following algorithm. + design

Cases:

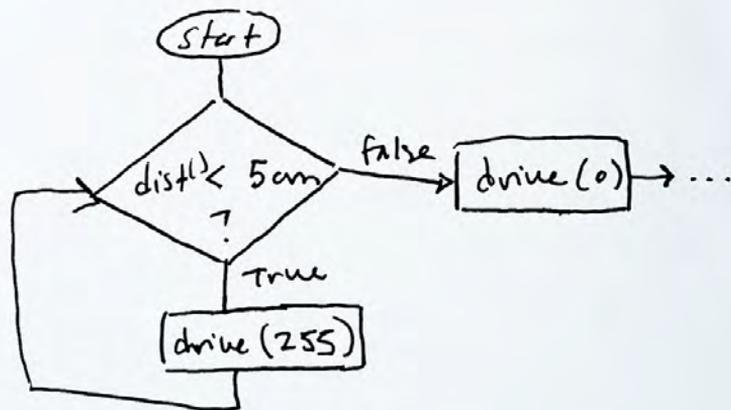


= Straight

⌊ inside

⌋ outside.

- which sensors / where do you put them?
- which filters do you use, why?
- what is the algo?
 - ↳ low level



why doesn't this "just work"?

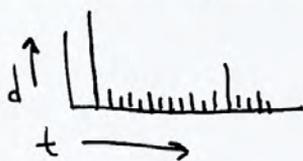
vs. PID version...

(5)

Shifting into a probabilistic
mindset...



How many measurements
until you're sure?



stability
of
signal

$$\Delta d = \text{change in } d = d_i - d_{i-1}$$

small Δd is small variation...
but also fragile!

$$\text{avg}(d_i : d_j) \quad \text{var}(\text{ ~~} d_i \text{ } : d_j) \quad \text{etc.}~~$$

⋮

$$P(\text{pos} \mid \text{measurement}) ?$$

$$\star \quad P(\text{pos})$$

$$P(\text{measurement}) ?$$